

[Total No. of Questions - 9] [Total No. of Printed Pages - 4]  
(2064)

14723

B. Tech 6th Semester Examination

Linear Control System (ECE/EEE)

EC-6004

Time : 3 Hours

Max. Marks : 100

The candidates shall limit their answers precisely within the answer-book (40 pages) issued to them and no supplementary/continuation sheet will be issued.

**Note :** Attempt five questions in all, by selecting one question from each section A, B, C, D and Section E. Question no. 9 is compulsory. All questions carry equal marks

**SECTION - A**

1. (a) What do you mean by sensitivity of the control system? Find  $S_G^T$  and  $S_H^T$  for the system shown in Fig. 1. (10)

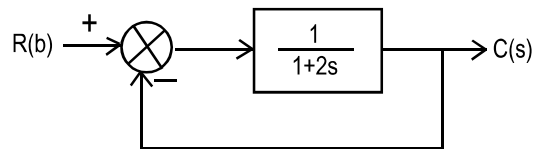


Fig. 1

- (b) Find the transfer function for the system shown in Fig. 2 [ $Y_1(s)/F(s)$ ]. (10)

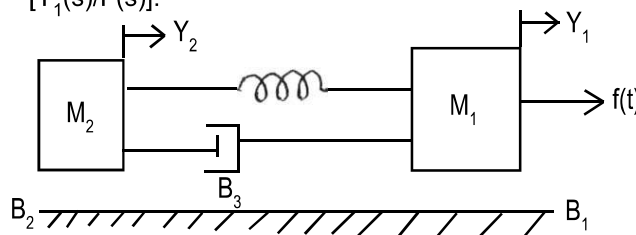


Fig. 2

2. (a) Find the transfer function  $C(s)/R(s)$  for the system shown in Fig. 3 by using block diagram reduction technique. (10)

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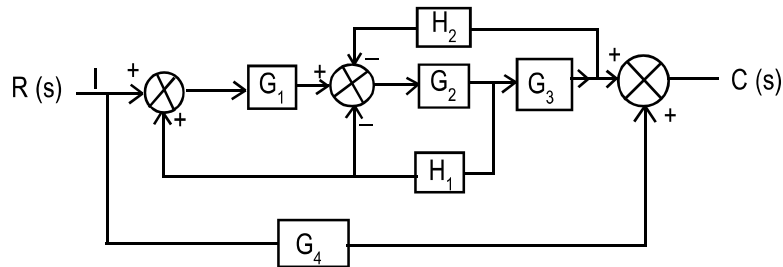


Fig. 3

- (b) The signal flow graph is shown in Fig 4. Find the transfer function. (10)

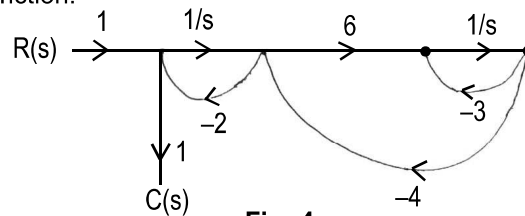


Fig. 4

## SECTION - B

3. (a) Explain settling time, rise time and maximum overshoot. For the system as shown in Fig. 5, find the rise time and settling time for this system. (10)

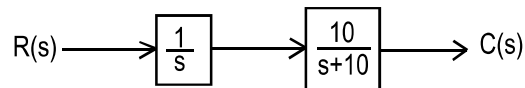


Fig. 5

- (b) The transfer function of a unity feedback system is given below:  
 $G(s) = (10^5(s+3)(s+10)(s+20))/(s(s+25)(s+a)(s+30))$   
 (i) Find type and order of the system.  
 (ii) Find the value of 'a' to yield velocity error constant  $k_v = 10^4$ . (10)
4. (a) The characteristics polynomial of a system is given as  $P(s) = 2s^5 + s^4 + 4s^3 + 2s^2 + 2s + 1$ . Determine the stability of the system. (10)
- (b) The unity feedback configuration with transfer function is given by  $G(s) = k(s^2 - 2s + 2)/(s^2 + 2s + 2)$ . Find the breakaway/ break in points and angle of departure when forward path gain  $k$  varies from  $-\infty$  to  $0$  ( $-\infty < k < 0$ ). (10)

## SECTION - C

5. (a) Find the steady state error for the plot shown in Fig. 6. (8)

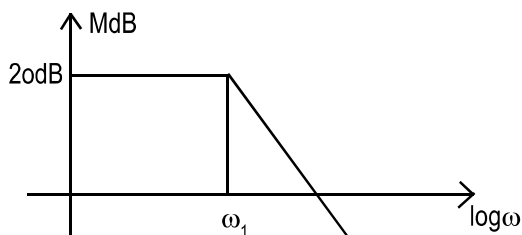


Fig. 6

- (b) Determine the gain margin (GM) and phase margin (PM) of the system with unity feedback, given as under:

$$G(s) = 1/(s(s+1)(1+.1s)) \quad (12)$$

6. (a) Draw the nyquist plot and determine the stability of the closed loop system.

$$G(s) H(s) = 1/(s^2(s+1)) \quad (12)$$

- (b) Explain M and N circle. (8)

## SECTION - D

7. (a) Write down the properties of state transition matrix. A linear system is described by the state equation shown in Fig. 7. Find the state transition matrix of the system. (10)

$$\dot{x}(t) = Ax(t) + Bu(t), \quad A = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$$

Fig. 7

- (b) The block diagram of a system with one input and two output  $y_1$  and  $y_2$  is given in Fig. 8. Determine the state space model of the system in terms of the state vector  $x$  and the output vector  $y = [y_1, y_2]^T$ . (10)

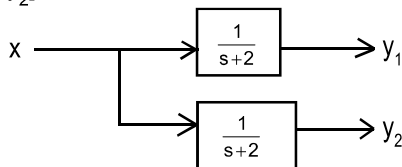


Fig. 8

8. (a) A transfer function of phase lead compensator is given by  
 $G(s) = (1 + 5T_s) / (1 + 2T_s)$ .  
 Find the maximum phase shift provided by such compensator.  
 Also draw the electrical network of the phase lead compensator.  
 (10)
- (b) Explain controllability and observability of the system. Determine the controllability and observability for the system by equations as shown in Fig. 9. (10)

$$\dot{x}(t) = Ax(t) + B u(t) \text{ and } y(t) = c x(t)$$

$$\text{where, } A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix},$$

$$C = [4 \quad 5 \quad 1]$$

Fig. 9

### SECTION - E (Compulsory)

9. (a) Define the transfer function.  
 (b) Derive the Laplace transform of  $\sin \omega t u(t)$ .  
 (c) Define state variables, state vector and state space.  
 (d) Briefly explain phase- variable form of the state-equation?  
 (e) Find the state equations and output equation for the phase - variable representation of the transfer function  $G(s) = (2s+1) / (s^2 + 7s + 9)$ .  
 (f) Give the pole-zero plot and response for  $G(s) = 9 / (s^2+9)$ ; when  $R(s) = 1/s$ .  
 (g) Considering the root locus diagram for a system with  $G(s) = K(s + 5) / (s (s+ 2) (s+ 4) (s^2+ 2s +2))$ , the meeting point of the asymptotes on the real axis occurs at \_\_\_\_\_?  
 (h) Find the steady state value for a control system if the Laplace transform of error  $e(t)$  is given as  $8(s+3)/s(s+10)$ . ( $8 \times 2.5 = 20$ )